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# 科研成果汇总

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2	Xu, XD; Bao, GQ; Ma, M; Wang, YW	[Xu, Xiaodong; Bao, Guangqing] Lanzhou Univ Technol, Coll Elect & Informat Engn, Lanzhou, Pcoples R China.; [Ma, Ming] State Grid Gansu Elect Power Corp, Wind Power Technol Ctr, Lanzhou, Peoples R China.; [Wang, Yuewu] Harbin Inst Technol, Sch Elect Engn & Automat, Harbin, Pcoples R China.	Multi-Objective Optimization Phase-Shift Control Strategy for Dual-Active-Bridge Isolated Bidirectional DC-DC Converter	INFORMACI MIDEM-JOU MICROELEC ELECTRONI COMPONEN MATERIALS 2021, 51 (3): 1	RNAL OF CTRONICS C TS AND	J Article	WOS:0007 088539000 03
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# **RESEARCH ARTICLE**

# Design of $H\infty$ Robust Controller With Load-Current Feedforward for Dual-Active-Bridge DC–DC Converters Considering Parameters Uncertainty

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**ABSTRACT** This paper proposes the design of  $H\infty$  robust controller with load-current feedforward for dual-active-bridge (DAB) dc-dc converters used in battery energy storage systems, aiming to ensure the dynamic response considering parameters uncertainty that the input voltage varies in a large range and the load is uncertain. Firstly, according to the state-space representation based on dual-phase-shift (DPS) control, a polytopic model of the DAB converter with two uncertain elements is established by convex optimization theory. Based on this model, linear matrix inequalities (LMIs) are then used to design the H $\infty$  robust controller conveniently to minimize the influence of parameters uncertainty disturbance on the output voltage. At the same time, a regional closed-loop pole configuration technique is used to guarantee the dynamic response of the system under a wide range of operating conditions. Furthermore, an improved load-current feedforward control with lookup tables for phase-shift compensation is adopted to further enhance the dynamic response. Finally, an OPAL-RT hardware-in-loop platform with Texas Instruments TMS320F28377D microcontroller is used to verify the feasibility and effectiveness of the proposed H $\infty$  robust controller.

**INDEX TERMS** Dual-active-bridge (DAB), dual-phase-shift (DPS), H∞controller, load-current feedforward, dynamic response.

## I. INTRODUCTION

Benefitting from some advantages such as symmetrical structure, bidirectional power transmission, soft-switching performance, and easy module cascade [1], [2], [3], [4], dual-active-bridge (DAB) dc-dc converter has been widely adopted in industrial applications, such as dc microgrids [5], power electronic transformers [6], distributed generation systems [7], battery energy storage systems (BESS) [8], and medium voltage AC/ DC hybrid power grid [9]. In the above

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applications, high power density and high efficiency are typical demands for the DAB converter. Especially in BESS, the DAB converter is simultaneously required to guarantee robust dynamic response under parameters uncertainty that the input voltage varies in a large range and the load is uncertain.

In recent years, many control schemes integrated with various phase-shift control strategies have been investigated to ensure the dynamic response of the DAB converter. In an early literature [10], dynamic response comparisons of traditional single-phase-shift (SPS), dual-phase-shift (DPS), and model-based phase-shift control (MPSC) for the DAB

converter are evaluated, with a conclusion that MPSC shows the best dynamic response. In [11], based on SPS control, a load-current feedforward (LCFF) compensation solution is presented to enhance the transient response of the DAB converter against the load change; however, the input voltage fluctuation is not considered. By introducing virtual direct power control (VDPC) into SPS control [12], a VDPC method is proposed to obtain zero overshoot and robust dynamic response when suffering load or input voltage transient disturbances. By combing improved MPSC with LCFF control for the SPS-controlled DAB converter, as presented in [13], the improved strategy can guarantee a faster dynamic response to all the operating ranges. Besides, a discrete extended-phase-shift (EPS) control with low computational complexity is proposed to achieve rapid dynamic response when both load and input voltage change [14]. Moreover, in order to reduce the load current sensor used in the above schemes to lower the hardware cost of the DAB converter. an extended state observer (ESO)-based sensor-reduction control with DPS [15] and a load-current estimating method with switching-period delay compensation [16] are proposed to boost dynamic responses.

Another method for dynamic response improvement for the DAB converter is to engage advanced control schemes, such as model predictive control (MPC), artificial neural network (ANN), sliding mode control,  $H\infty$  robust control and linear-quadratic regulator control. Combined with simple SPS, a non-linear MPC with phase-shift compensation is presented to enhance dynamic response against the disturbance of input voltage and load [17]. For DAB converter fast feeding constant power loads or pulsed power loads applied in dc microgrids, an ANN-based MPC method [18], a deep reinforcement learning-based intelligent nonlinear controller [19], an ANN-based active disturbance rejection control with ESO [20], and a moving discretized control set MPC (MDCS-MPC) with SPS [21] are proposed; however, they are extremely complex with a heavy computational burden. In order to lower the computational burden, by utilizing only two prediction horizons, an MDCS-MPC with triple-phase-shift (TPS) is proposed in [22]. Besides, though sliding mode control can provide the DAB converter with a fast transient response for load variations and robust control for parameter uncertainties [23], [24], heavy computation is still an issue. Similar to some advanced control schemes,  $H\infty$  robust controller is suited for improving the system stability and performance for power inverters/converters [25], [26], [27], [28], especially when the parameters are uncertain. However, few papers can be found on the application of the DAB converter. To effectively address the system uncertainty and parameter perturbations of the DAB converter, an H $\infty$  mixed sensitivity robust control is presented in [29], which finally obtains a third-order controller by solving Riccati equations, but the selection of the appropriate weighting function is a challenge. Furthermore, To cover such challenges, by using linear matrix inequalities (LMIs) to derive the optimized control parameters, an LMI

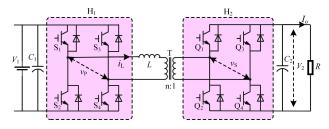


FIGURE 1. Topology configuration of DAB converter.

 $H\infty$  robust control is early used to design controllers for boost converters [30], but the disturbance of input voltage is not considered. And then, a robust LMIs-based linearquadratic regulator control for the DAB converter is improved in [31], which can enhance dynamic performances when both input voltage and load change and achieve robust stability. However, the above two robust controllers in [29] and [31] for the DAB converter are combined with SPS, lacking control freedom compared to DPS, EPS, or TPS.

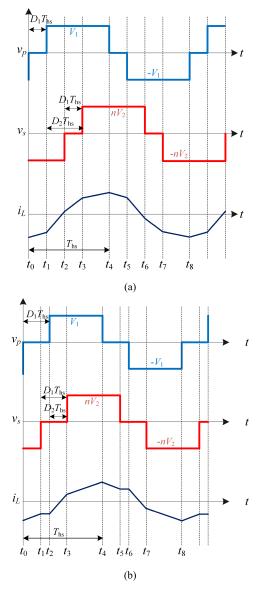
Thus, in this paper, for more control freedom, based on DPS control, an  $H\infty$  robust controller with LCFF for DAB dc-dc converters is proposed, aiming to ensure the dynamic response of the DAB converter considering parameters uncertainty that the input voltage varies in a large range and the load is uncertain. The main contribution of this paper is the establishment of a polytopic model for the DAB converter based on DPS control considering parameters uncertainty, so as to conveniently design the  $H\infty$  robust controller by using the LMIs to minimize the influence of parameters uncertainty disturbance on the output voltage. In addition, a regional closed-loop pole configuration technique based on LMIs is used to guarantee the acceptable dynamic response, while an LCFF with lookup tables for phase-shift compensation is improved to further enhance the dynamic response.

This paper is organized as follows. Firstly, a polytopic model of the DAB converter with two uncertain elements is established in Section II. Based on this model, LMIs are then used to design the H $\infty$  robust controller in Section III, with a regional closed-loop pole configuration technique to cope with the system under a wide range of input voltage conditions. Then, an improved LCFF control scheme is adopted to further ensure the dynamic response. Finally, Section IV provides the experimental results obtained from an OPAL-RT hardware-in-loop platform to verify the proposed H $\infty$  robust controller.

#### II. POLYTOPIC MODEL OF AN UNCERTAIN DAB CONVERTER UNDER DPS CONTROL

#### A. OPERATION PRINCIPLE AND SMALL-SIGNAL MODEL OF A DAB CONVERTER

Fig. 1 describes the topology of the DAB converter. Two full bridges  $H_1$  and  $H_2$  connect each other with an auxiliary inductor *L* and an isolated transformer (turn ratio n = 5:8 in this paper).  $C_1$  and  $C_2$  are the dc capacitors.  $S_1 \sim S_4$  and



**FIGURE 2.** Voltage and current waveforms of DAB converter under DPS control: (a)  $0 \le D_1 \le D_2 \le 1$ , (b)  $0 \le D_2 \le D_1 \le 1$ .

 $Q_1 \sim Q_4$  are two groups of switches in the two full bridges, respectively.  $V_1$  is the dc input voltage, and  $V_2$  is the dc output voltage.  $v_p$  and  $v_s$  represent the high frequency ac voltages generated by  $H_1$  and  $H_2$ , respectively.  $i_L$  is the inductor current, and  $I_o$  is the load current.

Generally, the DPS-based DAB converter has two degrees of freedom with inner phase-shift ratio and outer phase-shift ratio, which mainly operates in two modes [32]:  $0 \le D_1 \le D_2 \le 1$  and  $0 \le D_2 \le D_1 \le 1$ , as shown in Fig. 2.  $D_1$  represents the inner phase-shift ratio, which is the phase shift between switches  $S_1$  and  $S_4$  or  $Q_1$  and  $Q_4$ ;  $D_2$  represents the outer phase-shift ratio, which is the phase shift between switches  $S_1$  and  $Q_1$ ; and  $T_{1s}$  is half of the switching cycle. As shown in Fig. 2, under DPS control, the ac voltage output from two full bridges are three-level waves with an equal duty cycle and a specific phase shift. In the existing literature,  $D_1$  is usually used to improve the performances of the DAB converter, such as reactive power [33], current stress [34], and efficiency performance [35]; and  $D_2$  is obtained from a closed-loop control. In this paper,  $D_1$  is directly set to 0.2 for simplicity, so as to focus on the design of proposed H $\infty$  robust controller with  $D_2$ .

According to Fig. 1 and Fig. 2, in a switching cycle  $(T_s)$ , the DAB converter has eight operation modes. Moreover, the inductor current and the ac voltage of the two full bridges show symmetrical waveforms, so the state-space averaging model can be described in half a switching cycle.

In the DAB converter, when the condition meets  $0 \le D_1 \le D_2 \le 1$ , the inductor current at  $t_0$ ,  $t_1$ ,  $t_2$ ,  $t_3$ ,  $t_4$  can be described [36]:

$$\begin{cases} i_L(t_0) = \frac{V_1}{4f_sL}(D_1 - 1) - \frac{nV_2}{4f_sL}(2D_2 + D_1 - 1) \\ i_L(t_1) = \frac{V_1}{4f_sL}(D_1 - 1) + \frac{nV_2}{4f_sL}(1 + D_1 - 2D_2) \\ i_L(t_2) = \frac{V_1}{4f_sL}(2D_2 - D_1 - 1) + \frac{nV_2}{4f_sL}(1 - D_1) \\ i_L(t_3) = \frac{V_1}{4f_sL}(2D_2 + D_1 - 1) - \frac{nV_2}{4f_sL}(D_1 - 1) \\ i_L(t_4) = \frac{V_1}{4f_sL}(1 - D_1) + \frac{nV_2}{4f_sL}(2D_2 + D_1 - 1) \end{cases}$$
(1)

where  $f_s = 1/T_s$  is the switching frequency.

As can be seen from Fig. 1 and Fig. 2, it can be obtained four differential equations across the output capacitor  $C_2$  between each time interval of  $t_0 \sim t_4$  according to Kirchhoff current law:

$$\begin{cases} C_2 \frac{dv_2}{dt} = -\bar{i}_{L1} - \frac{v_2}{R} & t \in [0, D_1 T_{hs}] \\ C_2 \frac{dv_2}{dt} = -\bar{i}_{L2} - \frac{v_2}{R} & t \in [D_1 T_{hs}, D_2 T_{hs}] \\ C_2 \frac{dv_2}{dt} = -\frac{v_2}{R} & t \in [D_2 T_{hs}, (D_1 + D_2) T_{hs}] \\ C_2 \frac{dv_2}{dt} = -\bar{i}_{L4} - \frac{v_2}{R} & t \in [(D_1 + D_2) T_{hs}, T_{hs}] \end{cases}$$
(2)

where  $\bar{i}_{L1}$ ,  $\bar{i}_{L2}$ , and  $\bar{i}_{L4}$  represent the inductor current averaging values, which are:

$$\begin{cases} \bar{i}_{L1} = \frac{i_L(t_0) + i_L(t_1)}{2} \\ \bar{i}_{L2} = \frac{i_L(t_1) + i_L(t_2)}{2} \\ \bar{i}_{L4} = \frac{i_L(t_3) + i_L(t_4)}{2} \end{cases}$$
(3)

Furthermore, extending the four differential equations in (2) to the entire switching cycle of the DAB converter, timeaveraging scheme can be used to derive the final state-space averaging model:

$$C_2 \frac{dv_2}{dt} = \frac{nV_1}{4f_s L} [2d_2(1-d_2) - D_1^2] - \frac{v_2}{R}$$
(4)

where  $d_2$  is the outer phase-shift ratio containing ac disturbance.

In order to further derive the small-signal model of the DAB converter, low-frequency ac small-signal disturbance is introduced as

$$\begin{cases} v_2 = V_{2ss} + \hat{v}_2 \\ d_2 = D_{2ss} + \hat{d}_2 \end{cases}$$
(5)

where  $V_{2ss}$  and  $D_{2ss}$  are the dc component of the output voltage and outer phase-shift ratio, respectively, and  $\hat{v}_2$ and  $\hat{d}_2$  are the corresponding ac components, respectively. Substituting (4) into (5) and ignoring the small-signal ac component  $\hat{d}_2^2$ , the small-signal model of the DAB converter is derived as

$$\frac{d\hat{v}_2}{dt} = \frac{nV_1}{2f_s LC_2} (1 - 2D_{2ss})\hat{d}_2 - \frac{\hat{v}_2}{RC_2} \tag{6}$$

Aiming to guarantee accurate tracking control for the output voltage, another state variable  $x_2(t) = \int \left[ V_{ref} - v_2(t) \right] dt$  representing the integral of the corresponding voltage error is introduced. Thus, combining (5) and (6), the state-space representation of the DAB converter is written as

$$\dot{\mathbf{x}}(t) = \mathbf{A}\mathbf{x}(t) + \mathbf{B}_{w}w(t) + \mathbf{B}_{u}u(t) + \mathbf{B}_{ref}V_{ref}$$

$$z(t) = \mathbf{C}_{z}\mathbf{x}(t) + \mathbf{D}_{zw}w(t) + \mathbf{D}_{zu}u(t)$$
(7)

where  $\mathbf{x}(t) = \begin{bmatrix} v_2(t) \\ x_2(t) \end{bmatrix}$ ,  $w(t) = [i_o(t)]$ ,  $u(t) = [d_2(t)]$ ,  $z(t) = [v_2(t)]$ . The vector  $\mathbf{w}$  represents the disturbance of the load-current  $i_o$ . The output z represents the output voltage  $v_2$ . Moreover, the state-space matrices are as follows

$$\boldsymbol{A} = \begin{bmatrix} -\frac{1}{RC_2} & 0\\ -1 & 0 \end{bmatrix}, \quad \boldsymbol{B}_w = \begin{bmatrix} -\frac{1}{C_2}\\ 0 \end{bmatrix},$$
$$\boldsymbol{B}_u = \begin{bmatrix} \frac{nV_1}{2f_s LC_2}(1-2D_{2ss})\\ 0 \end{bmatrix}, \quad \boldsymbol{B}_{ref} = \begin{bmatrix} 0\\ 1 \end{bmatrix},$$
$$\boldsymbol{C}_z = \begin{bmatrix} 1 & 0 \end{bmatrix}, \quad \boldsymbol{D}_{zw} = \begin{bmatrix} 0 \end{bmatrix}, \quad \boldsymbol{D}_{zu} = \begin{bmatrix} 0 \end{bmatrix}$$
(8)

where A is the state matrix;  $B_w$  is the disturbance matrix;  $B_u$  is the control matrix;  $B_{ref}$  is the reference matrix;  $C_z$ ,  $D_{zw}$  and  $D_{zu}$  are output matrices.

Similarly, when the condition satisfies  $0 \le D_2 \le D_1 \le 1$ , the state-space averaging model is derived as

$$C_2 \frac{dv_2}{dt} = \frac{nV_1}{4f_s L} d_2 (2 - 2D_1 - d_2) - \frac{v_2}{R}$$
(9)

And the corresponding small-signal model of the DAB converter is derived as

$$\frac{d\hat{v}_2}{dt} = \frac{nV_1}{2f_s LC_2} (1 - D_1 - D_{2ss})\hat{d}_2 - \frac{\hat{v}_2}{RC_2}$$
(10)

So as the state-space matrices are obtained as

$$\boldsymbol{A} = \begin{bmatrix} -\frac{1}{RC_2} & 0\\ -1 & 0 \end{bmatrix}, \quad \boldsymbol{B}_w = \begin{bmatrix} -\frac{1}{C_2}\\ 0 \end{bmatrix},$$
$$\boldsymbol{B}_u = \begin{bmatrix} \frac{nV_1}{2f_sLC_2}(1 - D_1 - D_{2ss})\\ 0 \end{bmatrix}, \quad \boldsymbol{B}_{ref} = \begin{bmatrix} 0\\ 1 \end{bmatrix},$$
$$\boldsymbol{C}_z = \begin{bmatrix} 1 & 0 \end{bmatrix}, \quad \boldsymbol{D}_{zw} = \begin{bmatrix} 0 \end{bmatrix}, \quad \boldsymbol{D}_{zu} = \begin{bmatrix} 0 \end{bmatrix}$$
(11)

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## B. POLYTOPIC MODEL CONSIDERING THE UNCERTAINTY OF INPUT VOLTAGE AND LOAD

In BESS, considering that the terminal voltage varies widely during battery charging and discharging and the power transmitted to the dc bus depends on the load, that is, the input voltage  $V_1$  of the DAB converter is not a stable value, and the load is uncertain. Therefore, the polytopic model in convex optimization theory can be adopted to build the system model of the DAB converter so that LMI optimization methods can be easily applied to solve the closed-loop controller [30], [37]. This method ensures system stability at different operating points, as well as optimal immunity to disturbances and transient performance. In modelling, the input voltage and the load are taken as uncertainties, that is, a vector p = $(1/R, V_1)$  is used to include the two uncertain terms, which is constrained in the polytopic model. Thus, for the DAB converter, based on the state-space representation (7), the polytopic model can be formed as.

$$\begin{cases} \dot{\boldsymbol{x}}(t) = \boldsymbol{A}(\boldsymbol{p})\boldsymbol{x}(t) + \boldsymbol{B}_{w}\boldsymbol{w}(t) + \boldsymbol{B}_{u}(\boldsymbol{p})\boldsymbol{u}(t) + \boldsymbol{B}_{ref}V_{ref} \\ \boldsymbol{z}(t) = \boldsymbol{C}_{z}\boldsymbol{x}(t) + \boldsymbol{D}_{zw}\boldsymbol{w}(t) + \boldsymbol{D}_{zu}\boldsymbol{u}(t) \end{cases}$$
(12)

where the state-space matrices A(p) and  $B_u(p)$  are determined by uncertain terms grouped in the vector p. In this paper, A(p) and  $B_u(p)$  have a linear relationship with each uncertain parameter of vector p, respectively.

Generally, the introduced vector  $\boldsymbol{p}$  contains N uncertain parameters, that is  $\boldsymbol{p} = (p_1, p_2, \dots, p_N)$ . Each uncertain  $p_i$  is a bounded parameter, which is constrained within a specific range as

$$p_i \in \left[\underline{p}_i, \bar{p}_i\right] \tag{13}$$

Moreover, the possible values of vector  $\boldsymbol{p}$  are hold within a hyperrectangle in the parameter space  $\mathbb{R}^N$  with  $L = 2^N$  vertices  $\{v_1, v_2, \ldots, v_N\}$ . And the system matrix  $[\boldsymbol{A}(\boldsymbol{p}), \boldsymbol{B}_u(\boldsymbol{p})]$  for each vertex  $v_i$  corresponds to the extrema of a convex polytope, noted  $Co \{G_1, G_2, \ldots, G_L\}$ . Therefore, the system matrix  $[\boldsymbol{A}(\boldsymbol{p}), \boldsymbol{B}_u(\boldsymbol{p})]$  can be contained as

$$[\boldsymbol{A}(\boldsymbol{p}), \boldsymbol{B}_{u}(\boldsymbol{p})] \in Co\left\{G_{1}, G_{2}, \dots, G_{L}\right\}$$
$$:= \left\{\sum_{i=1}^{L} \lambda_{i} G_{i}, \lambda_{i} \geq 0, \sum_{i=1}^{L} \lambda_{i} = 1\right\} \quad (14)$$

A detailed description of the convex polytope can be found in [37] and [38].

When specific to this paper for the DAB converter, the input voltage  $V_1$  and the load resistance R are considered uncertainties (N = 2), while the rest elements are assumed constant. Thus, the two parameters of vector  $\mathbf{p} = (1/R, V_1)$  are constrained in the following boundaries:

$$1/R \in [1/R_{\max}, 1/R_{\min}], \quad V_1 \in [V_{1\min}, V_{1\max}]$$
 (15)

Furthermore, the polytopic model of the DAB converter established in this paper has  $L = 2^N = 4$  vertices that determine the uncertain matrices A(p) and  $B_u(p)$ . When the

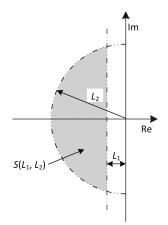


FIGURE 3. LMI region  $S(L_1, L_2)$ .

condition meets  $0 \le D_1 \le D_2 \le 1$ , the vertices are obtained as:

$$A_{1} = \begin{bmatrix} -\frac{1}{R_{\max}C_{2}} & 0\\ -1 & 0 \end{bmatrix}, \quad B_{u1} = \begin{bmatrix} \frac{nV_{1\min}}{2f_{s}LC_{2}}(1-2D_{2ss})\\ 0 \end{bmatrix},$$
$$A_{2} = \begin{bmatrix} -\frac{1}{R_{\min}C_{2}} & 0\\ -1 & 0 \end{bmatrix}, \quad B_{u2} = \begin{bmatrix} \frac{nV_{1\max}}{2f_{s}LC_{2}}(1-2D_{2ss})\\ 0 \end{bmatrix},$$
$$A_{3} = A_{2}, \quad B_{u3} = B_{u1},$$
$$A_{4} = A_{1}, \quad B_{u4} = B_{u2}$$
(16)

# III. PROPOSED $\text{H}\infty$ ROBUST SOLUTION WITH LOAD-CURRENT FEEDFORWARD

In this section, firstly,  $H\infty$  control is adopted to effectively suppress the influence of system parameter perturbation on output and minimize the gain of disturbance on output. Secondly, in order to improve the dynamic settling time of the system, the poles of the closed-loop system are configured in a specific region. In addition, an improved LCFF control is adopted to enhance the dynamic response.

#### A. $H\infty$ CONTROLLER BASED ON LMIS

For the polytopic model described in (12), there exists a statefeedback controller whose role is to achieve a minimum gain of the disturbance to the output. For the design of robust control systems, the gain of the disturbance to the output is usually transformed into the problem of  $H\infty$  norm bound. The  $H\infty$  norm can be explained by amplitude-frequency characteristics of a transfer function f(s), which is effective for problems related to model uncertainty. Considering that the transfer function from the disturbance w to the output z is H(s), the corresponding  $H\infty$  norm is expressed as

$$\|H(s)\|_{\infty} \sup_{w \neq 0} \frac{\|z\|_2}{\|w\|_2} \tag{17}$$

where  $\|\cdot\|_{\infty}$  represents the infinity norm and  $\|\cdot\|_2$  represents the Euclidian norm.

Considering that the smaller the  $H\infty$  norm, the better the suppression of the disturbance, when a minimum  $H\infty$  norm

 $\gamma$  is guaranteed, there exists a state-feedback H $\infty$  controller  $(u(t) = d_2(t) = Kx(t))$  if and only if a positive definite matrix  $W \in \mathbb{R}^{n \times n}$  and a matrix  $Y \in \mathbb{R}^{n \times n}$  make the following LMI hold

$$\begin{bmatrix} \boldsymbol{A}\boldsymbol{W} + \boldsymbol{W}\boldsymbol{A}^{\mathrm{T}} + \boldsymbol{B}_{\boldsymbol{u}}\boldsymbol{Y} + \boldsymbol{Y}^{\mathrm{T}}\boldsymbol{B}_{\boldsymbol{u}}^{\mathrm{T}} & \boldsymbol{B}_{\boldsymbol{w}} & \boldsymbol{W}\boldsymbol{C}_{\boldsymbol{z}}^{\mathrm{T}} + \boldsymbol{Y}^{\mathrm{T}}\boldsymbol{D}_{\boldsymbol{z}\boldsymbol{u}}^{\mathrm{T}} \\ \boldsymbol{B}_{\boldsymbol{w}}^{\mathrm{T}} & -\gamma\boldsymbol{I} & \boldsymbol{0} \\ \boldsymbol{C}_{\boldsymbol{z}}\boldsymbol{W} + \boldsymbol{D}_{\boldsymbol{z}\boldsymbol{u}}\boldsymbol{Y} & \boldsymbol{0} & -\gamma\boldsymbol{I} \end{bmatrix} < 0$$
(18)

Thus, the H $\infty$  controller is obtained by  $K = YW^{-1}$ . Proof of (18) can be found in [39]. For all the vertices  $\{G_1, G_2, \ldots, G_L\}$  in the polytopic model of the DAB converter, it is sufficient to satisfy (18) to solve the stability problem for different steady-state operating points of the system.

#### **B. POLE PLACEMENT LMIS**

In the classical control theory, the amplitude-frequency and phase-frequency characteristics of the open-loop system are obtained through the transfer function so as to design the controller according to the Bode diagram. However, the classical control method usually assigns the closed-loop poles precisely, which is not suite for the system with the imprecision of the model and the existence of various disturbances.

Thus, in this paper, LMI is used to directly assign the closed-loop poles of the system in a given region of the complex plane to ensure some desired dynamic characteristics, such as decay rate, settling time, damping ratio, etc. As shown in Fig. 3, in the region  $S(L_1, L_2)$  of the complex plane for the system [40], the assigned closed-loop poles  $(x \pm jy)$  should meet

$$x < -L_1 < 0, \quad |x \pm jy| < L_2$$
 (19)

where  $L_1$  and  $L_2$  are two values given by the designer.  $L_1$  is used to determine a minimum decay rate, and  $L_2$  is used to limit a maximum natural frequency.

Considering the decay rate constrained by  $L_1$ , the following LMI is obtained

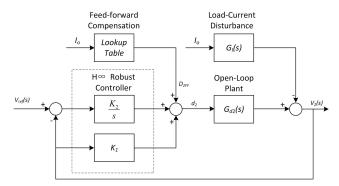
$$\boldsymbol{A}\boldsymbol{W} + \boldsymbol{W}\boldsymbol{A}^{\mathrm{T}} + \boldsymbol{B}_{\boldsymbol{u}}\boldsymbol{Y} + \boldsymbol{Y}^{\mathrm{T}}\boldsymbol{B}_{\boldsymbol{u}}^{\mathrm{T}} + 2L_{1}\boldsymbol{W} < 0 \qquad (20)$$

Furthermore, the constraint of the natural frequency according to  $L_2$  involves the following LMI

$$\begin{bmatrix} -L_2 W & W A^{\mathrm{T}} + Y^{\mathrm{T}} B_u^{\mathrm{T}} \\ A W + B_u Y & -L_2 W \end{bmatrix} < 0$$
(21)

A detailed explanation of LMIs (20) and (21) can be found in [40], and it is proven in [40] that when the system with the H $\infty$  robust controller  $u(t) = d_2(t) = \mathbf{K}x(t) = \mathbf{Y}\mathbf{W}^{-1}x(t)$ meets LMIs (20) and (21), the closed-loop poles ( $x \pm jy$ ) can be directly assigned in the given region  $S(L_1, L_2)$ .

Here, in this paper, all the vertices  $\{G_1, G_2, \ldots, G_L\}$  in the polytopic model of the DAB converter need to satisfy LMIs not only (18) but also (20) and (21), so that the closed-loop poles of the system under different stable operating points are



**FIGURE 4.**  $H\infty$  robust control with load-current feedforward compensation for DAB converter.

TABLE 1. Lookup tables for load-current feedforward compensation.

Input Voltage	250 V	300 V	350 V	400 V	450 V
$0 \leq D_1 \leq D_2 \leq 1$	0.0202	0.0169	0.0144	0.0126	0.0112
$0 \leq D_2 \leq D_1 \leq 1$	0.0171	0.0143	0.0122	0.0107	0.0095

assigned in the given region  $S(L_1, L_2)$  to meet the acceptable dynamic performance of the system.

Thus, by combining LMIs (18), (20) and (21), the LMI synthesis method for the proposed  $H\infty$  robust controller with pole placement can be summarized as the following optimization problem:

$$\min_{Y, W} \quad \gamma \quad \text{subject to (18), (20) and (21)} \\ \forall \{G_i\}, \quad i = 1, \dots, L$$
(22)

The solving procedure of the optimization problem (22) consists of finding a set of common matrices Y and W by solving LMIs, so as to obtain the H $\infty$  robust controller  $u(t) = d_2(t) = Kx(t) = YW^{-1}x(t)$ , which assigns the closed-loop poles of the system in the region  $S(L_1, L_2)$  and guarantees a minimum H $\infty$  norm  $\gamma$ .

#### C. LOAD-CURRENT FEEDFORWARD

In this section, an improved LCFF control is adopted to further enhance the dynamic response of the DAB converter, which treats the load-current as a feedforward compensation to the H $\infty$  robust controller without impact on the design of the controller. Such an idea applied to a DAB converter with SPS control was early proposed in [11], where feedforward compensation was adopted to feed forward a phase shift correction to regulate the output voltage when the loadcurrent changes. In this paper, a similar concept is adopted to cope with the uncertainties of the load resistance with DPS control.

To implement feedforward compensation, a relationship between the load-current and the commanded outer phaseshift ratio  $D'_2$  needs to be derived. According to the basic analysis of the DAB converter expressed in [34], the average

TABLE 2. DAB converter parameters in the HIL setup.	TABLE 2.	DAB convert	er parameters	in the	HIL setup.
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Symbol	Quantity	Value
$P_{\text{rated}}$	Converter Rated Power	5 kW
$V_1$	Input Voltage	$250~V\sim450~V$
$V_2$	Output Voltage	400 V
$f_{\rm s}$	Switching Frequency	2 kHz
$D_1$	Inner Phase-shift Ratio	0.2
п	Transformer Turn Ratio	5:8
L	Auxiliary Inductor Inductance	500 uH
$C_1, C_2$	DC Capacitance	1000 uF
$R_{ m min}$ , $R_{ m max}$	Load Resistance	$32~\Omega \sim 1000~\Omega$

transmission power with DPS control can be rewritten as

$$P = \begin{cases} \frac{nV_1V_2}{2f_sL} \left[ D_{2ol}^*(1 - D_{2ol}^*) - \frac{D_1^2}{2} \right], \\ 0 \le D_1 \le D_{2ol}^* \le 1 \\ \frac{nV_1V_2}{2f_sL} \left[ D_{2ol}^*(1 - D_1) - \frac{(D_{2ol}^*)^2}{2} \right], \\ 0 \le D_{2ol}^* \le D_1 \le 1 \end{cases}$$
(23)

where  $D_{2ol}^*$  is an open-loop commanded outer phase-shift ratio.

Thus, the load-current can be derived as

$$I_{o} = \begin{cases} \frac{nV_{1}}{2f_{s}L} \left[ D_{2ol}^{*}(1 - D_{2ol}^{*}) - \frac{1}{2}D_{1}^{2} \right], \\ 0 \le D_{1} \le D_{2ol}^{*} \le 1 \\ \frac{nV_{1}}{2f_{s}L} D_{2ol}^{*}(1 - D_{1} - \frac{1}{2}D_{2ol}^{*}), \\ 0 \le D_{2ol}^{*} \le D_{1} \le 1 \end{cases}$$
(24)

It can be seen from (24) that the relationship between the outer phase-shift ratio and the load-current is nonlinear, resulting in complicated inverting. However, for a certain input voltage  $V_1$ , one-to-one correspondence between the ideal outer phase-shift ratio  $D_{2ol}^* = D_{2FF}$  and any loadcurrent  $I_o$  can be precalculated as lookup tables, according to the condition  $0 \leq D_1 \leq D^*_{2ol} \leq 1$  or  $0 \leq D^*_{2ol} \leq$  $D_1 \leq 1$ . Considering that the input voltage ranges from 250 V to 450 V, the lookup tables are established every 50 V for a trade-off. Moreover, for a measured input voltage within the divided interval, a linear interpolation processing is adopted to calculate the target feedforward phase-shift compensation from the two adjacent lookup tables. Thus, in every control interrupt cycle, the controller can look up and calculate the new feedforward compensation for the next control cycle. Fig. 4 shows the block diagram of LCFF compensation implemented in an  $H\infty$  robust controller of the DAB converter. According to (24), the lookup tables are calculated and presented in Table 1.

#### **IV. EXPERIMENTAL VERIFICATION**

To verify the proposed design of  $H\infty$  robust controller, a realtime hardware-in-the-loop (HIL) platform is established. The

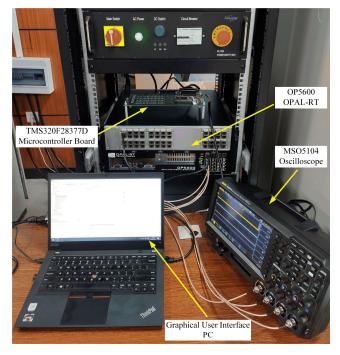


FIGURE 5. OPAL-RT real-time HIL platform with TMS320F28377D microcontroller board.

HIL setup is presented in Fig. 5, consisting of an OPAL-RT OP5600 real-time simulator and a powerful Texas Instruments TMS320F28377D Delfino microcontroller board. The DAB converter is built in the OP5600, and the proposed  $H\infty$  robust controller is implemented in the TMS320F28377D. The detailed parameters of the DAB converter in the HIL setup are presented in Table 2.

#### A. $H\infty$ CONTROLLER DESIGN

The control objective of the system is to obtain a minimum  $H\infty$  norm  $\gamma$  by assigning the closed-loop poles within the given region *S* ( $L_1$ ,  $L_2$ ) according to solving the optimization problem (22). In this paper, considering the minimum decay rate and the maximum natural frequency of the system,  $L_1$  can be set to 120, while  $L_2$  can be set to 1/20 of the switching frequency.

When the condition meets  $0 \le D_1 \le D_2 \le 1$ , by combining the detailed parameters in Table 2, the four vertices in the polytopic model of the DAB converter shown in (16) are calculated as

$$A_{1} = \begin{bmatrix} -1 & 0 \\ -1 & 0 \end{bmatrix}, \quad B_{u1} = \begin{bmatrix} 46875 \\ 0 \end{bmatrix}, A_{2} = \begin{bmatrix} -31.25 & 0 \\ -1 & 0 \end{bmatrix}, \quad B_{u2} = \begin{bmatrix} 115310 \\ 0 \end{bmatrix}, A_{3} = A_{2}, \quad B_{u3} = B_{u1}, A_{4} = A_{1}, \quad B_{u4} = B_{u2}$$
(25)

Then, the remaining disturbance matrix  $B_w$  is calculated as

$$\boldsymbol{B}_{w} = \begin{bmatrix} -1000\\ 0 \end{bmatrix} \tag{26}$$

Here, all the parameters and matrices used to solve the optimization problem (22) are obtained. With the help of MATLAB LMI toolbox, a total amount of fourteen LMIs can be formulated by introducing every vertex into (18), (20) and (21). The fourteen formulated LMIs consist of four LMIs from (18), four LMIs from (20), four LMIs from (21), one LMI from positive H $\infty$  norm  $\gamma$ , and one LMI from positive definite matrix W.

Take the LMIs of (18) for example, when the first vertex  $[A_1, B_{u1}]$  is introduced, the corresponding formulated LMI with MATLAB commands is expressed as

lmiterm([1 1 1 W],A1,1,'s'); lmiterm([1 1 1 Y],Bu1,1,'s'); lmiterm([1 1 2 0],Bw); lmiterm([1 1 3 W],1,Cz'); lmiterm([1 1 3 Y],1,Dzu'); lmiterm([1 2 2 gama],-1,1); lmiterm([1 3 3 gama],-1,1);

Thus, solving the optimization problem (22) by using MATLAB LMI toolbox, a set of common matrices Y and W can be found, obtaining the H $\infty$  controller K as

$$\boldsymbol{K} = \begin{bmatrix} K_1 & K_2 \end{bmatrix} = \begin{bmatrix} 0.0061 & 0.7969 \end{bmatrix}$$
(27)

and the H $\infty$  norm is  $\gamma = 6.9393$  (also known as 16.83 dB). The control law  $u(t) = d_2(t) = \mathbf{K}x(t)$  to yield the outer phase-shift ratio can be expressed as

$$d_2(t) = 0.0061v_2(t) + 0.7969x_2(t)$$
(28)

Similarly, when the condition meets  $0 \le D_2 \le D_1 \le 1$ , the control law to yield the outer phase-shift ratio can be obtained as

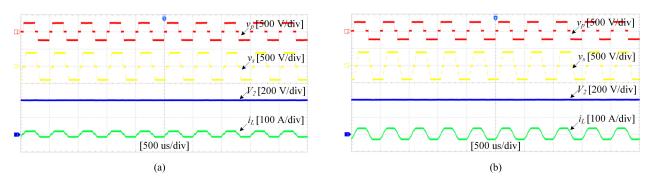
$$d_2(t) = 0.0071v_2(t) + 0.9491x_2(t)$$
<sup>(29)</sup>

#### **B. EXPERIMENTAL RESULTS**

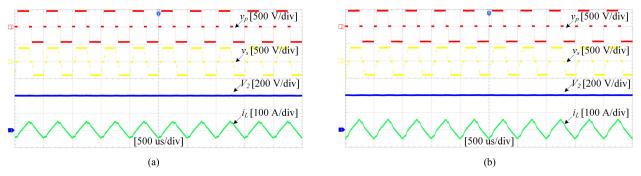
Fig. 6 shows the steady-state experimental waveforms under the proposed H $\infty$  robust controller when the primary side dc voltage  $V_1$  is 250 V. It is clear that the secondary side dc voltage  $V_2$  can be regulated at the designed 400 V under both half-load (R = 64  $\Omega$ ) and full-load (R = 32  $\Omega$ ). The full-bridge voltages  $v_p$  and  $v_s$  are high-frequency three-level waves with the effect of the inner phase-shift ratio, but the outer phase-shift ratio between  $v_p$  and  $v_s$  has a larger value under full-load in Fig. 6(b) compared with half-load in Fig. 6(a), due to more power needs to be transmitted under full-load.

Under the same load conditions, Fig. 7 shows the steadystate experiment waveforms under the proposed controller while the primary side dc voltage  $V_1$  is set to 450 V. According to Fig. 7, The secondary side dc voltage  $V_2$  is still regulated at the designed 400 V, and the outer phase-shift ratio has a larger value under full-load, while the waveforms of the auxiliary Inductor current  $i_L$  become triangle-like instead of trapezoid-like in Fig. 6, with higher peak values.

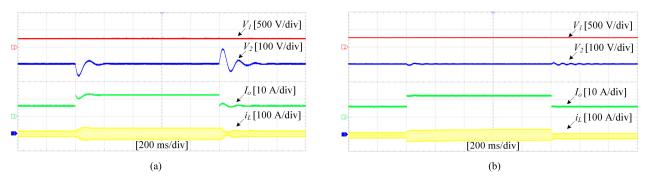
Fig. 8 shows the dynamic-state experimental comparison of the DAB converter under conventional and proposed



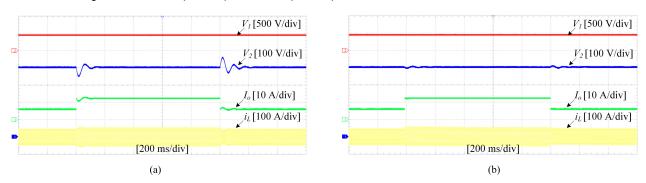
**FIGURE 6.** Steady-state experimental waveforms of DAB converter under the proposed controller when the primary side dc voltage is 250 V: (a) Half-load ( $R = 64 \Omega$ ), (b) Full-load ( $R = 32 \Omega$ ).



**FIGURE 7.** Steady-state experimental waveforms of DAB converter under the proposed controller when the primary side dc voltage is 450 V: (a) Half-load ( $R = 64 \Omega$ ), (b) Full-load ( $R = 32 \Omega$ ).



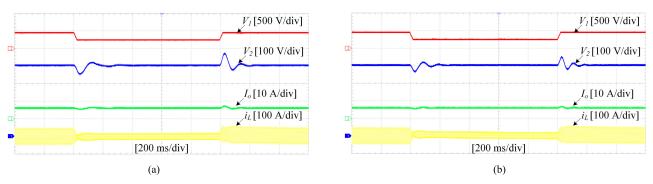
**FIGURE 8.** Dynamic-state experimental comparison of DAB converter under conventional and proposed controllers when the primary side dc voltage is 250 V: (a) Conventional controller with load switching between half-load ( $R = 64 \Omega$ ) and full-load ( $R = 32 \Omega$ ), (b) Proposed controller with load switching between half-load ( $R = 64 \Omega$ ) and full-load ( $R = 64 \Omega$ ) and full-load ( $R = 64 \Omega$ ).



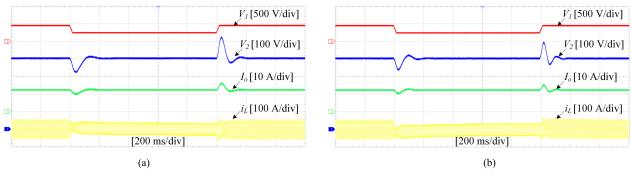
**FIGURE 9.** Dynamic-state experimental comparison of DAB converter under conventional and proposed controllers when the primary side dc voltage is 450 V: (a) Conventional controller with load switched between half-load ( $R = 64 \Omega$ ) and full-load ( $R = 32 \Omega$ ), (b) Proposed controller with load switched between half-load ( $R = 64 \Omega$ ) and full-load ( $R = 64 \Omega$ ).

controllers when the primary side dc voltage  $V_1$  is 250 V, and the load is switched between half-load and full-load.

According to Fig. 8(a), when the load is jumped from halfload to full-load by using the conventional PI controller,



**FIGURE 10.** Dynamic-state experimental comparison of DAB converter under conventional and proposed controllers with half-load condition ( $R = 64 \Omega$ ) and primary side dc voltage switching between 250 V and 450 V: (a) Conventional controller, (b) Proposed controller.



**FIGURE 11.** Dynamic-state experimental comparison of DAB converter under conventional and proposed controllers with full-load condition (R = 32 Ω) and primary side dc voltage switching between 250 V and 450 V: (a) Conventional controller, (b) Proposed controller.

the secondary side dc voltage  $V_2$  drops to 330 V, and the settling time takes almost 200 ms. However, as can be seen in Fig. 8(b), under the proposed controller, the experimental result shows satisfactory dynamic performances when switching between half-load and full-load, with slight voltage fluctuations and settling times.

Similar to Fig. 8, Fig. 9 shows the dynamic-state experimental comparison of the DAB converter under the conventional and proposed controllers while the primary side dc voltage  $V_1$  is set to 450 V. As shown in Fig. 9(a), it is obvious that the secondary side dc voltage  $V_2$  by using the conventional PI controller presents non-negligible voltage oscillations when the load varies, with a larger voltage fluctuation of 60 V and a longer settling time of 200 ms when the load is jumped from full-load to half-load. As a comparison in Fig. 9(b), the proposed controller shows excellent dynamic performances when switching between half-load and full-load, with negligible voltage fluctuations and settling times.

Fig. 10 and Fig. 11 show the dynamic-state experimental comparisons of the DAB converter under the conventional and proposed controllers with different load conditions and the change of primary side dc voltage. It can be seen that the effect of the proposed controller is mainly to reduce the amount of voltage fluctuation of the secondary side dc voltage  $V_2$ . Under the half-load condition, the voltage fluctuation of  $V_2$  can be reduced by about 15 V when the primary side dc voltage voltage  $V_1$  is switched between 250 V and 450 V. Moreover,

under the full-load condition, the voltage fluctuation of  $V_2$  can be reduced by almost 20 V.

According to Fig. 8 to Fig. 11, it can be concluded that the proposed  $H\infty$  robust controller achieves better dynamic response than the conventional PI controller when load resistance jumps and primary side dc voltage variations. Furthermore, over the entire primary side dc voltage range of 250 V to 450 V, it indicates that the proposed  $H\infty$ robust controller can achieve system stability and robustness whenever half-load or full-load.

## **V. CONCLUSION**

This paper presents the design of  $H\infty$  robust controller with load-current feed-forward for the DAB converter used in BESS. Based on DPS control, a polytopic model of the DAB converter with two uncertain elements is first established by convex optimization theory. LMIs are then used to design the H $\infty$  robust controller conveniently to minimize the influence of disturbance on the output voltage. To ensure the dynamic performance of the system under a wide range of operating voltage conditions, a regional closed-loop pole configuration technique is properly adopted. To further enhance the dynamic response, an improved LCFF control with lookup tables for phase-shift compensation is investigated. A series of comparative experiment results obtained from a built OPAL-RT hard-ware-in-loop platform verify that the proposed  $H\infty$  robust controller achieves robust and fast dynamic performance.

As a future work, an experimental prototype with the same rated power will be designed to further verify the performance of the proposed  $H\infty$  robust controller. And the application of  $H\infty$  robust control can be extended to the DAB converter with TPS control or other power converters.

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# Multi-Objective Optimization Phase-Shift Control Strategy for Dual-Active-Bridge Isolated Bidirectional DC-DC Converter

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**Abstract:** The dual-active-bridge isolated bidirectional DC-DC converter (DAB-IBDC) is a crucial device for galvanic isolation, voltage conversion, power transfer, and bus connection in the DC power conversion systems. Phase-shift modulation is an effective method to improve DAB-IBDC performance. However, the phase-shift control strategies in the previous literatures mainly focus on optimizing the characteristic of DAB-IBDC in a single aspect. In this paper, to optimize high-frequency-link (HFL) reactive power, current stress, and efficiency simultaneously, a new multi-objective optimization strategy based on dual-phase-shift (DPS) control is proposed. The power characterization, current stress, and power loss of the DAB-IBDC are analyzed. Besides, both the control principle and framework of the proposed control strategy are described in detail. Finally, the experiment results obtained from an established DAB-IBDC prototype are presented to verify the correctness and superiority of the proposed strategy.

Keywords: dual-active-bridge; multi-objective optimization; DPS control strategy; electrical performance

# Strategija upravljanja faznega premika z več ciljnimi optimizacijami za dvoaktivni izolirani mostič dvosmernega DC-DC pretvornika

**Izvleček:** Izolirani dvosmerni DC-DC (DAB-IBDC) pretvornik z dvoaktivnim mostičem je ključna naprava za galvansko izolacijo, pretvorbo napetosti, prenos moči in povezavo vodila v sistemih za pretvorbo enosmerne energije. Modulacija s faznim zamikom je učinkovita metoda za izboljšanje delovanja DAB-IBDC. Vendar se strategije nadzora s faznim zamikom v dosedanji literaturi osredotočajo predvsem na optimizacijo značilnosti DAB-IBDC z enega vidika. V tem članku je za hkratno optimizacijo jalove moči, tokovne napetosti in učinkovitosti visokofrekvenčne povezave (HFL) predlagana nova večpredmetna strategija optimizacije, ki temelji na nadzoru z dvojnim faznim zamikom (DPS). Analizirane so značilnosti moči, tokovne obremenitve in izgube moči DAB-IBDC. Poleg tega sta podrobno opisana tako načelo krmiljenja kot tudi okvir predlagane strategije krmiljenja. Na koncu so predstavljeni rezultati poskusov, pridobljeni iz vzpostavljenega prototipa DAB-IBDC, s katerimi sta preverjeni pravilnost in superiornost predlagane strategije.

Ključne besede: dvojni aktivni mostič; večnamenska optimizacija; strategija krmiljenja DPS; električna zmogljivost

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# 1 Introduction

With the wide application of direct-current (DC) renewable power sources, DC loads, and storage equipment, DC power conversion systems (PCS) have considerable potential for engineering applications [1-4]. With the development of power electronics, isolated bidirectional DC-DC converters (IBDCs) have become popular for galvanic isolation, voltage conversion, and power transfer in DC PCS [5-6]. Among various IBDCs, the du-

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The improvements of DAB-IBDC in the previous literatures mainly focus on the topology design and optimization, mathematical model derivation, phase-shift modulation strategies, converter control schemes, and soft-switching realization [11-15]. Particularly, the phase-shift control is an effective method to optimize the DAB-IBDC performance [16]. The phase-shift control strategies can be categorized into single-phaseshift (SPS), extended-phase-shift (EPS), dual-phaseshift (DPS), and triple-phase-shift (TPS). With DAB configurations each full bridge is driven with specific phase-shift. While these phase-shifts can differ in DPS they are equal and referred as inner phase-shift, and phase-shift between each full bridge is the outer phaseshift [7]. The SPS has one degree of freedom with outer phase-shift, and the EPS and DPS have two degrees of freedom with inner phase-shift and outer phase-shift, while the TPS has three degrees of freedom with two different inner phase-shifts and an outer phase-shift. In [17], an improved asymmetric modulation for both-side of DAB-IBDC is proposed, enabling the smooth transaction during steady-state operation and minimizing the transient time regardless of equivalent resistance of inductor. In [18], optimized phase-shift modulations are proposed to accelerate the transient response and suppress the DC bias during transient process. In [19-20], a mathematical model of current stress for DAB-IBDC is established, and the minimum current stresses are achieved under DPS and TPS control strategies, respectively. In [21-22], the DAB-IBDCs with soft-switching operation during whole operating range are analyzed, expanding the zero-voltage switching (ZVS) range and promoting efficiency. In [23-24], the power loss and efficiency models are established, and the efficiency optimized modulation schemes based on phase-shift control are developed. Other phase-shift modulation strategies are also proposed in [25-28] to eliminate reactive power, reduce the peak and root-mean-square (RMS) values of HFL current, and enhance light-load performance for DAB-IBDC, respectively. Moreover, the phase-shift strategies with quasi-square-wave, triangle-wave and sine-wave modulation are investigated for improving performance under varied modulation methods [29-30]. Besides, the TPS control strategy is an

efficient method to improve the performance of DAB [31-33].

The phase-shift control strategies in the previous literatures have improved the performance of DAB-IBDC effectively. However, most existing phase-shift control strategies only realize the performance optimization in a single aspect (e.g., current stress, reactive power elimination, ZVS behavior, or efficiency performance of DAB-IBDC). The phase-shift control strategy for multiobjective optimization, i.e., simultaneously optimizes various characteristics of DAB-IBDC, has not been considered and discussed yet. Besides, some phaseshift control strategies with optimal phase-shift angle contain lots of electrical parameters, nonlinear equations, or trigonometric calculation, leading to a high computational burden, a complicated process, and a poor real-time characteristic in practical application. In this paper, to address the above problems and achieve the comprehensive optimization for DAB-IBDC, a multiobjective optimization strategy with DPS control is proposed. The proposed strategy can reduce current stress, improve transmission power, and minimize power loss simultaneously. Consequently, the proposed strategy can achieve high efficiency and improve adaptability and practicality for DAB-IBDC, which promotes the application of DAB-IBDC and also accelerates the development of DC PCS.

This paper is organized as follows. The topology, switching behavior based on DPS control, and the performance characteristics including the high-frequencylink (HFL) current stress, power factor, and power loss of the DAB-IBDC are investigated in Section 2. On this basis, a multi-objective optimization based on DPS control is proposed in Section 3. Then, Section 4 provides the experimental results obtained from a built DAB-IBDC prototype to verify the proposed strategy.

# 2 Performance characteristics of DAB-IBDC under DPS control

The topology of the DAB-IBDC is presented in Fig. 1. The DAB-IBDC is consisted of active full-bridges H<sub>1</sub> and H<sub>2</sub>, two DC capacitors C<sub>1</sub> and C<sub>2</sub>, an auxiliary inductor L<sub>1</sub> and an high-frequency-link (HFL) transformer with a conversion ratio n. S<sub>1</sub> ~ S<sub>4</sub> and D<sub>1</sub> ~ D<sub>4</sub> are switches and diodes in H<sub>1</sub>, respectively, and Q<sub>1</sub> ~ Q<sub>4</sub> and M<sub>1</sub> ~ M<sub>4</sub> are switches and diodes in H<sub>2</sub>, respectively. V<sub>1</sub> and V<sub>2</sub> are DC voltages on two sides of DAB-IBDC, respectively. The energy transfer could be equivalent to the transmission of energy between two modulated voltage sources through equivalent inductor L. i<sub>L</sub> is HFL current flowing through the equivalent inductor. v<sub>p</sub> is the HFL voltage on the primary side.  $v_s$  is the HFL voltage on the secondary side, which is generated by secondary terminate and equivalent to the primary-side voltage.

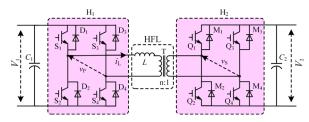
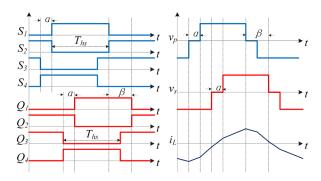


Figure 1: Topology configuration of DAB-IBDC.



**Figure 2:** The operation principle, HFL voltages, and currents under DPS control.

Generally, the DPS control has two working modes: the inner phase-shift ratio is larger or smaller than the outer phase-shift ratio, which is determined by the transferred power [7]. Different from EPS and TPS, the inner phase-shift ratios under DPS strategy in active full-bridges on both sides are the same.  $T_s$  is the switching period. To avoid the analysis complexity brought from the traditional time-domain segmentation function, the unified model form based on the Fourier series is applied in the analysis and control design. According to the topology of DAB-IBDC, the operation principle, HFL voltages, and currents under DPS control are presented in Fig. 2, where  $\beta$  is the outer phase-shift angle between  $v_p$  and  $v_s$ , and  $\alpha_1 = \alpha_2 = \alpha$  is the inner phase-shift angle.

According to Fourier series, the primary and secondary side HFL voltages  $v_{p}$  and  $v_{s'}$  shown in Fig. 2, are:

$$\begin{cases} v_p(t) = \sum_{k=1,3,5\dots} \frac{4V_1}{k\pi} \cos(\frac{k\alpha}{2}) \sin(n\omega t) \\ v_s(t) = \sum_{k=1,3,5\dots} \frac{4V_2}{k\pi} \cos(\frac{k\alpha}{2}) \sin[n(\omega t - \beta)] \end{cases}$$
(1)

Since the average inductor current is equal to zero during steady-state, the HFL current  $i_{L}$  in every switching period can be express as:

$$i_{L}(t) = \int_{t_{0}}^{t} \frac{v_{P}(t) - v_{S}(t)}{L} dt + i_{L}(t_{0})$$
<sup>(2)</sup>

From (1) - (2), the following equations can be obtained:

$$\begin{cases} i_{L}(t) = \sum_{k=1,3,5\dots} \frac{4}{k^{2} \pi \omega L} \sqrt{A^{2} + B^{2}} \sin(k\omega t + \arctan\frac{A}{B}) \\ A = \cos(\frac{k\alpha}{2}) [V_{2}\cos(k\beta) - V_{1}] \\ B = V_{2}\cos(\frac{k\alpha}{2})\sin(k\beta) \end{cases}$$
(3)

Thus, the root-mean-square (RMS) value of  $i_1$  is:

$$I_{L-RMS} = \sqrt{\sum_{k=1,3,5,\dots} I_{Lk}^{2}} = \sqrt{\sum_{k=1,3,5,\dots} \left[\frac{2\sqrt{2}}{k^{2}\pi\omega L}\sqrt{A^{2} + B^{2}}\right]^{2}}$$
(4)

## 2.1 Transmission power characterization

The average transmission power P can be obtained as:

$$P = \frac{1}{T_{hs}} \int_0^{T_{hs}} v_p(t) \bullet i_L(t) dt$$
<sup>(5)</sup>

Substituting (1) - (3) into (5), the average transmission power P can be further calculated as:

$$P = \sum_{k=1,3,5\dots} \frac{8V_1 V_2}{k^3 \pi^2 \omega L} \cos^2(\frac{k\alpha}{2}) \sin(k\beta)$$
(6)

Besides, the reactive power Q can be obtained:

$$\begin{cases} Q_{k_1=k_2=k} = \sum_{k=1,3,5\dots} \frac{8V_1 \cos^2(\frac{k\alpha}{2})}{k^3 \pi^2 \omega L} [V_1 - V_2 \cos(k\beta)] \\ Q_{k_1 \neq k_2} = U_{ak_1} I_{Lk_2} = \frac{8V_1}{k_1 k_2^2 \pi^2 \omega L} \cos(\frac{k\alpha}{2}) \sqrt{A^2 + B^2} \end{cases}$$
(7)

From (6) - (7), the apparent power S is calculated as:

$$S = \sqrt{\sum_{k=1,3,5...} P_k^2 + \sum_{k=1,3,5...} Q_k^2 + \sum_{k=1,3,5...} Q_{k_1 \neq k_2}^2}$$
(8)

Finally, the HFL power factor  $\lambda$  can be obtained as:

$$\lambda = P / S \tag{9}$$

Based on (6) - (9), Fig. 3 shows the HFL power factors under conventional control strategy. In Fig. 3, the HFL power factor  $\lambda$  is influenced by phase-shift angles, and the HFL power factors under DPS are higher. Besides, under DPS (DPS<sub>1</sub> < DPS<sub>2</sub> < DPS<sub>3</sub>), with the increasing of inner angle  $\alpha$ , the HFL power factor  $\lambda$  becomes higher correspondingly, decreasing HFL reactive power and increasing efficiency of DAB-IBDC.

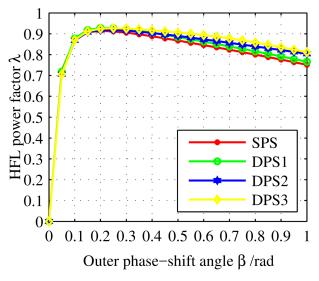


Figure 3: HFL power factors of DAB-IBDC.

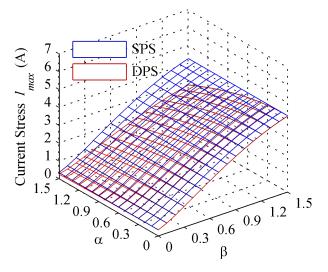


Figure 4: The current stress of DAB-IBDC.

## 2.2 Current stress characterization

To prolong the service life of switching devices, and improve the efficiency of DAB-IBDC, reducing the current stress is an effective solution. In the DAB-IBDC, the maximum value of HFL current  $i_{\rm L}$  represents the current stress. From (3), it can be observed that the HFL current  $i_{\rm L}$  compromises components with different frequencies under Fourier series analysis. Since the fundamental component in HFL current  $i_{\rm L1}$  is approximated with HFL current  $i_{\rm L}$  during operation, the maximum value of the fundamental component of  $i_{\rm L}$  can be considered as the current stress  $I_{\rm max}$ :

$$I_{\max} = \max\{|i_{L1}(t)|\} = \frac{2V_2 \cos(\frac{\alpha}{2})\sqrt{1 + M^2 - 2M\cos(\beta)}}{\pi\omega L}$$
(10)

where  $M = V_1 / nV_2$  is the voltage conversion ratio of DAB-IBDC.

According to (10), the current stress is closely related to  $V_1$ ,  $V_2$ ,  $\alpha$ ,  $\beta$ , and M. Fig. 4 presents the current stress  $I_{max}$  with the different  $\alpha$  and  $\beta$  under the SPS and DPS control. From Fig. 4, it can be observed: 1) with the increase of outer  $\beta$ , the current stress  $I_{max}$  increases under these two strategies, 2) under the same outer  $\beta$ , the current stress produced by DPS control is kept smaller. Besides, the current stress can be reduced with the increase of phase-shift  $\alpha$  under DPS.

#### 2.3 Power loss characterization

For DAB-IBDC, its total power loss  $P_{\text{LOSS}}$  mainly contains conducting loss  $P_{\text{CON'}}$  switching loss  $P_{\text{SW'}}$  and loss of magnetic components  $P_{\text{TA}}$  [24].

$$P_{\rm LOSS} = P_{\rm CON} + P_{\rm SW} + P_{\rm TA} \tag{11}$$

(1) Conducting loss: From the topology of DAB-IBDC, the conducting loss  $P_{\rm CON}$  is the sum of conducting losses in switches and diodes namely  $P_{\text{CONS}}$  and  $P_{\text{COND'}}$  respectively. For the DAB-IBDC, the dead-band loss should be considered and could not be ignored. As the zero-voltage-switching (ZVS) for DAB-IBDC can be also realized by using the freewheeling of anti-parallel diodes during dead-band time. Thus, the dead-band current is freewheeling in diodes, which means the deadband loss can be considered as a part of conducting loss. For simplicity, assume that the diodes and switches in DAB-IBDC have the same conducting resistance  $R_{\rm CON}$ . Besides, the conducting loss is closely related to the RMS HFL current in primary bridge H<sub>1</sub> and secondary bridge H<sub>2</sub> namely  $I_1$  and  $I_2$ , respectively. The relationship between  $I_1$  and  $I_2$  is  $I_1 = I_2 / n = I / \sqrt{2}$ . Consequently, the conducting loss of switches and diodes in a switching period are:

$$P_{\rm CON} = 4R_{\rm CON}I_1^2 + 4R_{\rm CON}I_2^2 = 2(1+n^2)R_{\rm CON}I_{\rm L-RMS}^2$$
(12)

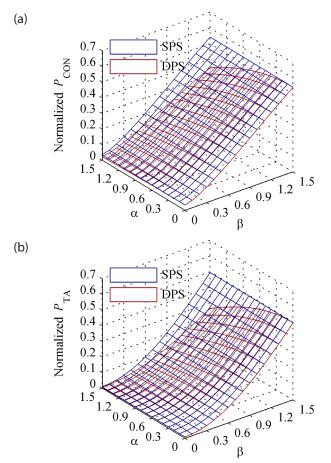
Based on (12), the conduction losses  $P_{\rm CON}$  is mainly decided by RMS current  $I_{\rm L-RMS}$  of HFL. Under both SPS and DPS control, the conduction loss  $P_{\rm CON}$  for DAB-IBDC are presented in Fig. 5(a), and they are normalized by  $P_{\rm CON} = 2(1 + n^2) R_{\rm CON} I_{\rm L-max}^2$ . Obviously, with the increase of phase-shift angle  $\beta$ , the conduction loss  $P_{\rm CON}$  increases, while  $P_{\rm CON}$  under DPS is always smaller. Besides, the conduction loss  $P_{\rm CON}$  drops with the increase of inner phase-shift  $\alpha$ .

(2) Switching loss: From [24], with the same transfer power, switching loss is relatively smaller compared with the conducting loss and the loss of magnetic components, and it only accounts for a small proportion of the overall power loss of DAB-IBDC. Besides, under soft-switching achievement, the switching loss can be neglected. Thus, for simplicity, the switching loss is ignored here. (3) Loss of magnetic components: In DAB-IBDC, magnetic components include the transformer and the auxiliary inductor. Typically, the power loss of magnetic component consists of the copper loss and core loss. Assuming that the winding resistance of magnetic components is constant, the copper loss  $P_{\text{COPP}}$  is closely related to the RMS value of  $i_{\rm L}$ . In addition, the RMS value of  $i_{\rm L}$  also plays a major role in the core loss  $P_{\text{CORE}}$ . The power loss of magnetic components  $P_{\text{TA}}$  can be obtained as:

$$P_{\rm TA} = P_{\rm COPP} + P_{\rm CORE} = (R_{\rm tr} + R_{\rm au} + \frac{2mf_s\mu_0^2N^2V_e}{g^2})I_{\rm L-RMS}^2$$
(13)

where  $R_{tr}$  is the transformer winding resistance while  $R_{au}$  is auxiliary inductor winding resistance. *m* represents the specific parameter of core loss,  $\mu_0$  represents the permeability of vacuum, *N* represents the number of turns,  $V_e$  represents the effective core volume, and *g* represents the air gap of magnetic path.

Based on (13), the power loss  $P_{\text{TA}}$  is affected by the RMS current  $I_{\text{L-RMS}}$  of HFL. Fig. 5(b) shows the curves of normalized power loss of magnetic components  $P_{\text{TA}}$  for DAB-IBDC under DPS, in which they are normalized by



**Figure 5:** The power loss for DAB-IBDC. (a) Conducting loss, (b) Loss of magnetic components.

 $P_{TA} = (R_{tr} + R_{au} + 2mf_s u_0^2 N^2 V_e / g_2) I_{L-max}^2$ . It is obvious that, the power loss  $P_{TA}$  increases with the raise of outer angle  $\beta$ , which is smaller under DPS compared with SPS. Besides, the  $P_{TA}$  reduces with the raise of the inner angle  $\alpha$ .

# 3 Multi-objective optimized strategy based on DPS control

From the analysis above, in the DAB-IBDC, all the HFL reactive power, current stress, and efficiency performance could be optimized by DPS strategy simultaneously. Accordingly, an optimized strategy based on DPS control is investigated for DAB-IBDC.

The current stress  $I_{max'}$  conducting loss  $P_{CON'}$  and loss of magnetic components  $P_{TA}$  are:

$$\begin{cases} I_{\text{max}} = I_{L} = \sqrt{2}I_{\text{L-RMS}} \\ P_{\text{con}} = 2(1+n^{2})R_{\text{CON}}I_{\text{L-RMS}}^{2} \\ P_{\text{TA}} = (R_{\text{tr}} + R_{au} + \frac{2mf_{s}\mu_{0}^{2}N^{2}V_{e}}{g^{2}})I_{\text{L-RMS}}^{2} \end{cases}$$
(14)

From (14), it could be seen that the current stress of DAB-IBDC is affected by the RMS value of HFL current  $I_{L-RMS}$ . Besides, the conducting loss  $P_{CON}$  and loss of magnetic components  $P_{TA}$  are also mainly affected by the RMS current of HFL. Thus, through optimizing the HFL current, the current stress, power loss, and the efficiency can be all optimized. Once the optimal RMS value of HFL current is obtained, the optimization of current stress and efficiency for DAB-IBDC could be realized at the same time.

To obtain the optimal RMS value of HFL current, a Lagrangian objective function is constructed:

$$E(\alpha, \beta, \lambda) = I_{\text{L-RMS}}(\alpha, \beta) + \lambda(P(\alpha, \beta) - P_0)$$
(15)

where  $P_0$  is the calculated output power for DAB-IBDC, which is obtained through multiplying the reference output voltage  $V_{2ref}$  by the output current  $I_2$ . Substituting (6) and (10) into (15), the constraints of the optimal equation can be obtained as:

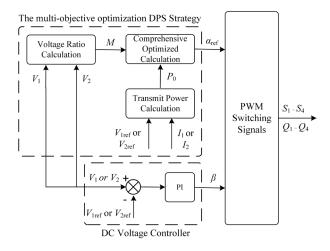
$$E = \frac{2nV_2\cos(\frac{\alpha}{2})\sqrt{1+M^2-2M\cos(\beta)}}{\pi\omega L} + \lambda[\frac{4V_1V_2n}{\pi^2\omega L}\cos^2(\frac{\alpha}{2})\sin(\beta) - P_0]$$
  
$$\frac{\partial E}{\partial \alpha} = \sqrt{1+M^2-2M\cos(\beta)} + \frac{4\lambda V_1}{\pi}\cos(\frac{\alpha}{2})\sin(\beta) = 0$$
(16)  
$$\frac{\partial E}{\partial \beta} = \frac{M\sin(\beta)}{\sqrt{1+M^2-2M\cos(\beta)}} + \frac{2\lambda V_1}{\pi}\cos(\frac{\alpha}{2})\cos(\beta) = 0$$
  
$$\frac{\partial E}{\partial \lambda} = \frac{4V_1V_2n}{\pi^2\omega L}\cos^2(\frac{\alpha}{2})\sin(\beta) - P_0 = 0$$

From (15) and (16), the optimal solution ( $\alpha$ ,  $\beta$ ) for DAB-IBDC under DPS control can be obtained by the results of the nonlinear equations in (16), and the DPS-based optimized strategy for DAB-IBDC is presented in Fig. 6. For the proposed strategy, the outer angle  $\beta$  is obtained from the output voltage control loop. An optimized calculation model is used to obtain the inner angle  $\alpha$  for reducing the current stress/power loss and improving the efficiency of DAB-IBDC.

From (16), the common solution and Pareto front of optimization for inner angle  $\alpha$  is further obtained:

$$\alpha = \arccos \sqrt{\frac{P_0 \pi^2 \omega L}{n V_1 V_2 \sin(\beta)}}$$
(17)

From (17), since the fluctuations in switching frequency and inductance value are very small compared with the magnitude of normalized transmission power and DC voltages, their influence on optimization result will be very small. Therefore, the optimal inner phase-shift angle  $\alpha$  is mainly determined by outer phase-shift angle  $\beta$ , relatively fixed parameters normalized transmission power  $P_{\alpha}$ , the HFL voltage ratio n, and also DC voltages  $V_1$  and  $V_2$ .



**Figure 6:** Control framework of proposed multi-objective optimized DPS strategy for DAB-IBDC.

# 4 Experiment verification

To verify the proposed control strategy, a 1kW rated DAB-IBDC prototype is established, and the load power rating is rated 1kW. The detailed parameters are presented in Table 1, and the prototype is shown in Fig. 7.

 Table 1: Parameters of DAB-IBDC Prototype.

Parameters	Value	Symbol
Primary Side DC Voltage	50V ~ 150V	<b>V</b> <sub>1</sub>
Secondary Side DC Voltage	50V ~ 150V	V <sub>2</sub>
Switching Frequency	20kHz	fs
Transformer Turn Ratio	1:1	n
HFL Equivalent Inductor	30uH	L
DC-link Capacitance	150uF	C <sub>1</sub> , C <sub>2</sub>
Load Resistance	10Ω ~ 100Ω	R

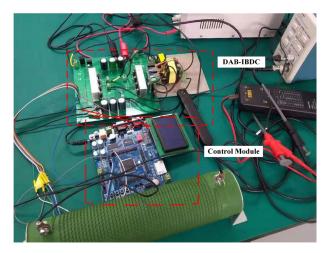
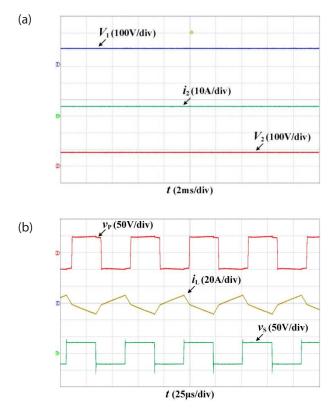
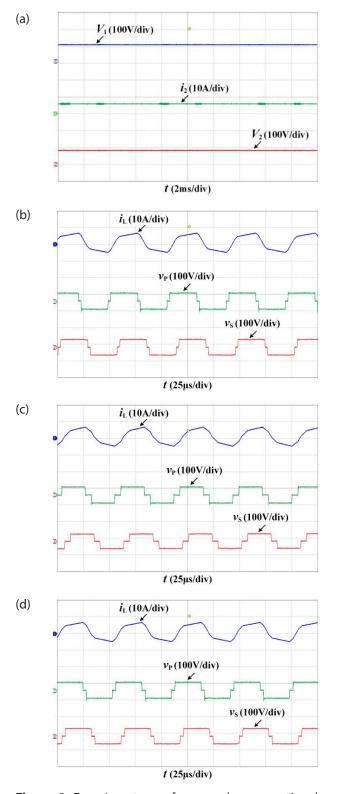


Figure 7: The prototype of DAB-IBDC.



**Figure 8:** Experiment waveforms under SPS. (a) DC side voltages and current, (b) HFL voltages and current.

For the DAB-IBDC, Fig. 8 shows the steady-state experiment waveforms under SPS control. It can be seen that,

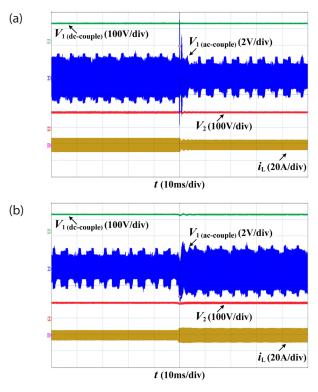


**Figure 9:** Experiment waveforms under conventional and proposed optimized DPS. (a) DC side Voltages and current of DAB-IBDC, (b) Conventional DPS when  $\alpha = 0.12$ , (c) Conventional DPS when  $\alpha = 0.25$ , (d) Proposed optimized DPS when  $\alpha = 0.18$ .

the  $V_1$  on the primary DC side is 100V, and the  $V_2$  on the secondary DC side is regulated at the designed 80V. The HFL voltages  $v_p$  and  $v_s$  are both high-frequency square waves, and the frequencies of  $v_p$ ,  $v_s$  and  $i_L$  are 20kHz. Besides, since the DC voltages deviate from the conversion ratio 1:1, the HFL current stress and reactive power become high. However, the SPS control could not solve this issue, and the maximum value of HFL current is 10.1A.

With the same transmission power, Fig. 9(a) and Fig. 9(b) show the experiment waveforms of DAB-IBDC under the conventional DPS control. It can be seen that the DAB-IBDC operates normally, i.e.,  $V_1$  is 100V and  $V_2$  is also regulated at the designed 80V. Besides, the HFL current stress and reactive power under DPS control are lower than that under SPS control. Thus, the DPS strategy is able to improve the performance of the DAB-IBDC by reducing the maximum value of HFL current to 9.4A. Moreover, steady-state experiment waveforms of HFL current under conventional DPS and proposed optimized control are presented in Fig. 9(c) and Fig. 9(d). It can be seen that the conventional DPS with a larger

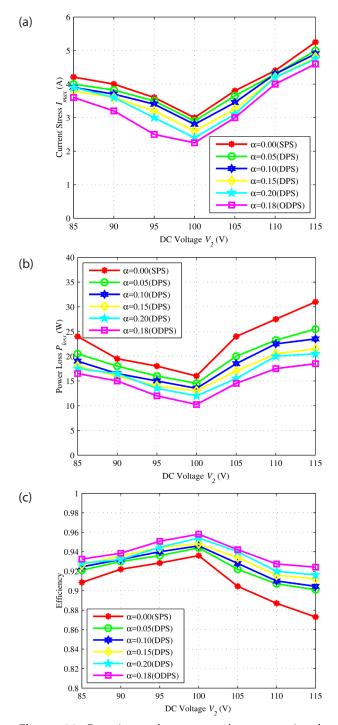
inner phase-shift angle can further reduce the HFL current stress and reactive power, and the value of HFL current under the proposed optimized DPS control can reduce to 8.7A. Accordingly, the HFL current stress and reactive power under proposed optimized DPS control



**Figure 10:** The dynamic-state experiment waveforms of DAB-IBDC under proposed optimized DPS strategy. (a) Load varies from 100% to 50%; (b) Load varies from 50% to 100%.

are lowest compared with that under SPS and conventional DPS.

The dynamic-state waveforms of the DAB-IBDC under the proposed optimized DPS strategy are presented in Fig. 10. According to Fig. 10(a), when the load varies from 100% to 50%, the voltage ripple of  $V_1$  decreases,



**Figure 11:** Experimental curves under conventional strategies and proposed optimized DPS (ODPS) strategy. (a) Curves of current stress, (b) Curves of power loss, (c) Curves of efficiency.

and  $V_2$  maintains at 100V. Besides, the HFL current stress  $i_{\rm L}$  decreases correspondingly. Similarly, when the load varies from 50% to 100%, the voltage ripple of  $V_1$  increases, and  $V_2$  keeps at 100V. In addition, the HFL current stress  $i_{\rm L}$  increases correspondingly, according to Fig. 10(b). Based on the above analysis, it can be concluded that under the proposed optimized DPS strategy, the DC voltages on both sides of DAB-IBDC maintain at designed value, and the DAB-IBDC operates stably during the dynamic-state.

With the same transmission power and varied DC voltages, Fig. 11(a) shows the current stress of DAB-IBDC under conventional strategies and proposed optimized control strategy. From Fig. 11(a), it can be observed that: under the three control strategies, the lowest current stress occurs when V1 = V2 = 100V. However, the current stress would become higher because the conversion ratio deviates from 1:1 farther (e.g., V2 drops from 100V to 85V or increases from 100V to 115V). Also, the current stress under DPS control is lower than that under SPS control, and increasing the inner phase-shift angle can further reduce the current stress. In addition, the proposed optimized DPS strategy achieves the lowest current stress for DAB-IBDC among the three strategies.

Similarly, Fig. 11(b) and Fig. 11(c) present the power loss and efficiency of DAB-IBDC under conventional control strategies and proposed optimized control strategy, respectively. Similar to the results of current stress experiments, under various phase-shift control strategies, the lowest power loss can be achieved when V1 = V2 =100V. Once V2 varies and deviates from the conversion ratio 1:1, it would result in larger power loss and lower efficiency. Meanwhile, lower power loss is achieved by the DPS strategy compared with that under the SPS strategy. Increasing the inner phase-shift angle  $\alpha$  can further reduce power loss. In addition, the proposed optimized strategy realizes the lowest power loss, so as to obtain the highest efficiency for DAB-IBDC. Thus, the proposed multi-objective optimized strategy improves the efficiency of DAB-IBDC.

# 5 Conclusions

The DAB-IBDC plays a crucial role in DC distribution networks for realizing galvanic isolation, voltage conversion, power transfer, and bus connection. In this paper, the effect of phase-shift control on power transmission characteristic, current stress, and efficiency of DAB-IB-DC is analyzed in detail. Then, to optimize these three features simultaneously, a DPS-based multi-objective optimized control strategy is proposed. The experiment results obtained from a built DAB-IBDC prototype verify that 1) the DPS control realizes less HFL reactive power, lower current stress, and higher efficiency for DAB-IBDC compared with SPS control, 2) the proposed optimized DPS control strategy optimizes the three features of DAB-IBDC simultaneously. Accordingly, the proposed control strategy can effectively improve the performance of DAB-IBDC, which makes it more adaptable and practical in DC power conversion networks.

# 6 Acknowledgments

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# 7 Conflict of interest

The authors declare no conflict of interest. The founding sponsors had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, and in the decision to publish the results.

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# 应用于模块化多电平直流变换器的阶梯波 调制策略

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摘要:在直流配电网中,模块化多电平直流变换器 MDCC(modular multilevel DC/DC converter)以模块化多 电平变换器结构为基础,是实现不同电压等级直流母线电压变换和电能双向传输的核心装置。探讨 MDCC 的高 频链阶梯波调制策略,并采用傅里叶级数建模,可有效简化阶梯波建模和分析过程。此外,阶梯波调制可有效减 小高频链电压 dv/dt、谐波和无功含量,提升 MDCC 整体效率,促进 MDCC 在直流配电网中的应用。 关键词:直流配电网;模块化多电平直流变换器;阶梯波调制

# Staircase Triangular Modulation Strategy for Modular Multilevel DC/DC Converter

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**Abstract**: In a DC distribution network, based on the structure of a modular multilevel converter(MMC), the modular multilevel DC/DC converter(MDCC) is a key device for realizing the voltage conversion and bidirectional power transmission between DC buses of different voltage levels. The staircase triangular modulation(STM) strategy for high-frequency link(HFL) in MDCC is analyzed. With Fourier series, the modeling and analysis process of STM can be effectively simplified. In addition, STM can effectively reduce the dv/dt and content of harmonics and reactive power in HFL voltages, improving the overall efficiency of MDCC and promoting its applications in DC distribution network.

Keywords: DC distribution network; modular multilevel DC/DC converter; staircase triangular modulation

随着分布式电源的发展,直流配电网可以发挥 直流配电的技术优势,有效减少不必要的转换环

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Project Supported by National Natural Science Foundation of China(51967012); Scientific Research and Innovation Team Project of Gansu Education Department(2018C-09); State Grid Gansu Electric Power Company Project(SGGSKY00FJJS1800142) 节,方便新能源、储能系统和直流负荷的接入,降低 配电系统的复杂程度和成本,改善电能质量,提高 电能转换和传输效率,因而已成为学术界和电力行 业的重要研究课题<sup>[1-3]</sup>。其中,直流变压器 DCT(DC transformer) 是实现直流配电网不同电压等级直流 母线电压变换和电能双向传输的核心装置<sup>[4-5]</sup>。

在低压小功率领域,DCT 最普遍采用的是双有 源全桥 DAB(dual active bridge)拓扑结构<sup>[68]</sup>。为了 提升DCT 的电压等级和功率容量,有效进行电压变

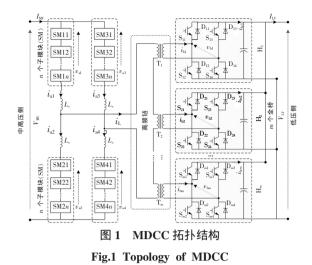
换及电能传输, 在模块化多电平变换器 MMC(modular multilevel converter)拓扑结构的基础上提出的 模块化多电平直流变换器 MDCC(modular multilevel DC/DC converter)备受关注<sup>[9-10]</sup>。为更好地连接中高 压与低压直流母线,文献[11]提出了一种基于 MMC 和全桥变换器结构的 MDCC 拓扑,目前,对于 MD-CC 的研究主要集中于拓扑结构、控制方法、高频链 HFL(high-frequency link)调制和联网运行等。其中, 方波调制是 HFL 调制常用的调制方式, 可有效提 升直流电压利用率和功率传输能力,但也因此造成 较大 dv/dt, 而且方波电压存在大量谐波和无功成 分,降低变换器效率,不利于推广应用<sup>112</sup>;此外,阶梯 波调制可有效减轻变压器上的 dv/dt 应力, 并降低 HFL 电压中的谐波含量,对基于 MMC 的模块化多 电平直流变换器的 HFL 调制有了初步的探讨[13-14]。 然而,对于 MDCC 这种不对称拓扑的直流变换器的 阶梯波调制仍未见报道。

本文将阶梯波调制方式应用到 MDCC 的 HFL 调制中,并采用傅里叶级数建模,可有效简化阶梯 波调制方式的建模和分析过程。此外,采用阶梯波 调制方式,可有效减小 HFL 电压的 dv/dt、谐波和无 功含量,提升 MDCC 整体效率,更好地在直流配电 网中实现电压变换和电能传输。

# 1 MDCC 的 HFL 阶梯波调制

# 1.1 MDCC 拓扑结构

本文所采用的 MDCC 拓扑结构如图 1 所示。 MDCC 中高压侧采用单相 MMC 结构,每个桥臂由 *n* 个半桥子模块 SM(sub-module)和 1 个电感 *L*<sub>s</sub> 串 联而成,可有效提高电压和功率等级;低压侧采用 *m* 个全桥变换器并联,以提升电流等级;高频链由 多个高频隔离变压器串联而成。MDCC 半桥 SM 和 全桥变换器的数量都可以根据实际应用中电压和 功率等级进行调整。*V*<sub>MV</sub> 和 *I*<sub>MV</sub> 分别为中高压侧电



压和电流, $V_{\rm LV}$ 和 $I_{\rm LV}$ 分别为低压侧电压和电流; $v_{\rm aij}$ 和 $V_{\rm ij}$ 分别为半桥子模块在交流侧和直流侧的电压, $v_{\rm ai} \sim v_{\rm a4}$ 和 $i_{\rm a1} \sim i_{\rm a4}$ 分别为 MMC 桥臂电压和电流; $i_{\rm L}$ 为高频链电流; $v_{\rm bi}$ 和 $i_{\rm bi}$ 分别为全桥模块交流侧电压和电流, $i_{\rm bci}$ 为全桥模块直流侧电流。

为了产生理想的 HFL 阶梯波,在中高压侧 MMC 结构的同一桥臂相邻的 SM 之间加入  $\pi/n$  的 移相角,在低压侧相邻全桥变换器之间加入  $\pi/n$  的 移相角。子模块电压叠加形成桥臂电压,从而形成 高频链电压  $v_{a}$ ;全桥模块电压  $v_{b}$  形成高频链电压  $v_{b}$ ;2 个高频链电压的差加在高频电感上产生高频 链电流  $i_{Lo}$  为保证子模块间直流侧电压的平衡,本 文采用文献[15]所提子模块电压交替平衡算法,有效 降低了电压平衡算法的复杂度。

1.2 MDCC 阶梯波调制建模与特性分析

MDCC 结构和控制复杂,使时域分析中产生的 波形分段过多,为避免因此导致的分段函数复杂且 难以分析和计算的问题,采用傅里叶级数变换方 法,使得 HFL 调制的分析从时域转到频域,进行 HFL 电气量分析和数学建模。

采用傅里叶级数进行描述,HFL 电压 v<sub>a</sub>和 v<sub>b</sub> 可分别表示为

$$\begin{cases} v_{a}(t) = \sum_{k=1,3,5,\cdots} \frac{4V_{MV}}{kn\pi} \cos\left(\frac{k\alpha_{1}}{2}\right) \sum_{i=0}^{n-1} \sin\left[k\left(\omega t + i\frac{\pi}{n}\right)\right] = \sum_{k=1,3,5,\cdots} \frac{4V_{MV}}{k\pi n} \cos\left(\frac{k\alpha_{1}}{2}\right) \frac{\sin\left(\frac{k\pi}{2}\right) \sin k\left[\omega t + \frac{(n-1)\pi}{2n}\right]}{\sin\left(\frac{k\pi}{2}\right)} \\ v_{b}(t) = \sum_{k=1,3,5,\cdots} \frac{4n_{T}V_{LV}}{k\pi} \cos\left(\frac{k\alpha_{2}}{2}\right) \sum_{i=0}^{n-1} \sin\left[k\left(\omega t - \beta + i\frac{\pi}{m}\right)\right] = \sum_{k=1,3,5,\cdots} \frac{4n_{T}V_{LV}}{k\pi} \cos\left(\frac{k\alpha_{2}}{2}\right) \frac{\sin\left(\frac{k\pi}{2}\right) \sin k\left[\omega t - \beta + \frac{(m-1)\pi}{2m}\right]}{\sin\left(\frac{k\pi}{2m}\right)}$$
(1)

式中: $n_{\rm T}$ 为高频链变压器电压变比;n为子模块数;  $\alpha_1$ 和  $\alpha_2$ 为内相移角;  $\beta$ 为初级和次级 HFL 电压之 间的相移角。当 $\alpha_1 = \alpha_2 = 0$ 时为单移相控制SPS(single-phase shift);当  $\alpha_1 = 0$ ,  $\alpha_2 \neq 0$  或  $\alpha_2 = 0$ ,  $\alpha_1 \neq 0$  时为 扩展移相控制 EPS(extend-phase shift);当  $\alpha_1 = \alpha_2 = \alpha_1$ 时为双移相控制 DPS(dual-phase shift)。

应用于 MDCC 的阶梯波调制波形见图 2, 开关 频率  $f_{s}=20$  kHz。由图可知, HFL 电压阶跃被限制为 1 个 SM 或全桥变换器模块电压,有效地降低了  $dv/dt_{o}$ 

此外,MDCC 可等效为2个交流电压源连接在 电感两端,且根据 HFL 电流在1个开关周期的对 称性,HFL 电流可表示为

$$i_{\rm L}(t) - i_{\rm L}(0) = \int_0^t \frac{v_{\rm a}(t) - v_{\rm b}(t)}{L} dt$$
 (2)

结合稳态条件时电感电流开关周期平均值为 0,由式(1)可得 HFL 电流为

$$i_{\rm L}(t) = \sum_{k=1,3,5,\cdots} \frac{2\sin\left(\frac{k\pi}{2}\right)}{k^2 \pi \omega L} \sqrt{A^2 + B^2} \sin\left(k\omega t + \arctan\frac{A}{B}\right)$$

$$A = \cos\left(\frac{k\alpha_2}{2}\right) n_{\rm T} V_{\rm LV} m \cos k \left[-\beta + \frac{(m-1)\pi}{2m}\right] - \cos\left(\frac{k\alpha_1}{2}\right) V_{\rm MV} \cos k \frac{(n-1)\pi}{2n} \qquad (3)$$

$$B = -\cos\left(\frac{k\alpha_2}{2}\right) n_{\rm T} V_{\rm LV} m \sin k \left[-\beta + \frac{(m-1)\pi}{2m}\right] + \cos\left(\frac{k\alpha_1}{2}\right) V_{\rm MV} \sin k \frac{(n-1)\pi}{2n}$$

 $v_{s}$ V.r v<sub>a3</sub> v <sub>a33</sub>  $\pi/n$  $v_{a11}$ v<sub>al2</sub> V .13 V .41 v .4

(a)中高压侧 MMC 子模块调制波形

图 2 HFL 阶梯波调制波形

 $\pi/m$ 

 $\pi/n$ 

Fig.2 Waveforms of HFL under staircase triangular modulation

在平衡的三相系统中,由于对称关系,偶次谐 波被消除得非常小、所以主要存在的是奇次谐波。 因此,除了基波分量外,HFL 电压和电流主要含有 奇次谐波分量,HFL 电压电流和有效值可以分别描 述为

$$\begin{cases} V_{\text{arms}} = \sqrt{\sum_{k=1,3,5,\cdots} V_{ak}^2} = \sqrt{\sum_{k=1,3,5,\cdots} \left[ \frac{2\sqrt{2} V_{\text{MV}}}{kn\pi \sin\left(\frac{k\pi}{2n}\right)} \right]^2} \\ V_{\text{brms}} = \sqrt{\sum_{k=1,3,5,\cdots} V_{bk}^2} = \sqrt{\sum_{k=1,3,5,\cdots} \left[ \frac{2\sqrt{2} n_{\text{T}} V_{\text{LV}}}{k\pi \sin\left(\frac{k\pi}{2m}\right)} \right]^2} \\ I_{\text{arms}} = \sqrt{\sum_{k=1,3,5,\cdots} I_k^2} = \sqrt{\sum_{k=1,3,5,\cdots} \left( \frac{2\sqrt{2}}{k^2 \pi w_0 L} \sqrt{A^2 + B^2} \right)^2} \end{cases}$$
(4)

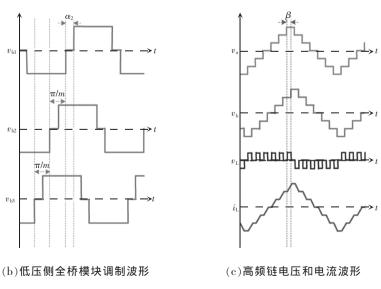
由式(1)~式(4)可得,1个开关周期内 MDCC 的平均传输功率为

$$P = \frac{1}{T} \int_{0}^{T} v_{a}(t) i_{L}(t) dt$$
(5)

由此,有功功率仅仅是由相同频率的电压和电 流分量产生,可以表示为

$$P = \sum_{k=1,3,5,\cdots} \frac{4V_{\rm MV} V_{\rm LV} n_{\rm T} m \, \sin^2\left(\frac{k\pi}{2}\right)}{k^3 \pi^2 \omega L} \cos\left(\frac{k\alpha_1}{2}\right) \cdot \cos\left(\frac{k\alpha_2}{2}\right) \sin(k\beta) \tag{6}$$

无功功率可以通过相同频率和不同频率的电 压和电流分量来产生,即



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 $v_{\rm b}$ 

 $v_{\rm b}$ 

(7)

$$\begin{cases} Q_{k_1 \neq k_2 = k} = \sum_{k=1,3,5,\dots} \frac{4V_{\text{MV}}V_{\text{LV}}n_{\text{T}}m \sin^2\left(\frac{k\pi}{2}\right)}{k^3\pi^2\omega L} \cos\left(\frac{k\alpha_1}{2}\right) \cdot \\ \left[M \cos\left(\frac{k\alpha_1}{2}\right) - \cos\left(\frac{k\alpha_2}{2}\right)\cos(k\beta)\right] \\ Q_{k_1 \neq k_2} = U_{ak_1}I_{lk_2} = \frac{4V_{\text{MV}}\sin^2\left(\frac{k_1\pi}{2}\right)}{k_1k_2^2\pi^2\omega L}\cos\left(\frac{k_1\alpha_1}{2}\right) \cdot \\ \sqrt{A^2 + B^2} \end{cases}$$

式中:M为 MDCC 的电压变换比, $M=V_{MV}/mn_TV_{LV\circ}$ 

由式(5)~式(7)可得 MDCC 的视在功率 S 为

$$S = \sqrt{\sum_{k=1,3,5,\cdots} P_k^2} + \sum_{k=1,3,5,\cdots} Q_k^2 + \sum_{k=1,3,5,\cdots} Q_{k,k=k_2}^2$$
(8)

因此,由式(5)~式(8)可得 MDCC 的 HFL 功率 因数为

$$\lambda = \frac{P}{S} \tag{9}$$

由式(1)可看出,采用阶梯波调制,HFL 电压波 形接近正弦波,电压的谐波含量降低;进而由式(3) ~式(7)可得无功功率含量也相应降低。此外,根据 式(7)~式(9),外移相角 $\beta$ 及内移相角 $\alpha(\alpha_1=\alpha_2=\alpha)$ 对 HFL 功率因数的影响如图 3 所示,选取  $\alpha=0$  对 应 SPS 控制, $\alpha=0.2$  对应 DPS 控制。可以看出,通过 调节外移相角和内移相角,能有效调节 MDCC 的传 输功率、无功功率和功率因数,从而进一步抑制 HFL 谐波和无功功率,降低损耗,提升 MDCC 整体 效率。

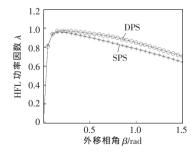


图 3 MDCC 的 HFL 功率特性

Fig.3 HFL power characteristics of MDCC

# 2 实验验证

为了有效验证理论分析,在实验室环境搭建了

1台 MDCC 样机,如图 4 所示,其参数如表 1 所示。

采用阶梯波调制时,稳态下 MDCC 的实验波形 如图 5 所示。可见,MDCC 中高压侧电压稳定在 300 V;低压侧电压稳定在 130 V;HFL 电压  $v_a$  和  $v_b$ 均为阶梯波, $v_a$ 、 $v_b$  和电流  $i_L$  的频率均为 20 kHz。对 比方波调制,阶梯波调制的 HFL 电压接近正弦波, 且随着 SM 和全桥变换器数量的增加,高频链电压 愈发呈现正弦波状;其 HFL 电压的谐波含量也大 为降低。

采用阶梯波调制时,MDCC 两端的 SM 和全桥 变换器电压波形如图 6 所示。从图中可以看出,各 SM 方波电压  $v_{a11}, v_{a12}, v_{a13}$  的幅值相等,均为 $V_{de}$ ;且相 邻 SM 电压的相角差为  $\pi/3$ ,使得 HFL 电压  $v_a$  呈阶 梯波升降。区别于传统方波调制,阶梯波调制使每 个 SM 电压幅值下降为  $V_{MV}/n=300/3=100$  V,加在 HFL 变压器的 dv/dt 也从方波调制的300 V 下降为 阶梯波调制的 100 V,有效降低了高频电压的 dv/dt以及开关管的压降。其次,低压侧的全桥变换器产 生相同幅值的方波电压  $v_{b1}$ , $v_{b2}$ 和 $v_{b3}$ ,并直接构成 HFL 电压  $v_{b0}$ 最后,构成 MDCC 的SM 和全桥变换器

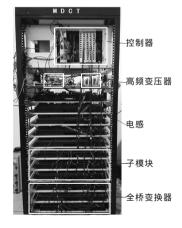


图 4 MDCC 实验样机

Fig.4 Experimental prototype of MDCC

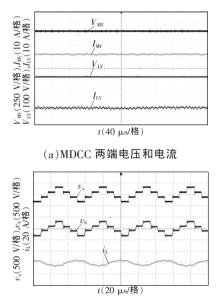
表1 实验样机参数

Tab.1 Parameters of experimental prototype

参数	数值	参数	数值
高压侧电压/V	300	变压器漏感/μH	42
低压侧电压/V	115~145	桥臂电感/μH	31
开关频率/kHz	20	变压器变比	4:5
桥臂子模块数	3	子模块电容/μF	470

均处于均压状态,确保了 MDCC 的正常运行。

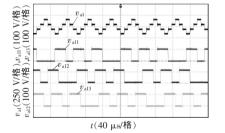
阶梯波调制下,当低压侧电压变化时,选择不 同内移相角 α 的 MDCC 整体效率如图 7 所示。由 图可知,当低压侧电压为 130 V 时,MDCC 两端电



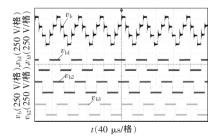
(b)HFL 电压和电流



operation under staircase triangular modulation



(a)中高压侧 SM 电压



(b)低压侧全桥变换器电压

图 6 阶梯波调制下 MDCC 两端 SM 和全桥变换器电压 Fig.6 Voltages of SMs at two terminals of MDCC and full-bridge converter under staircase triangular modulation

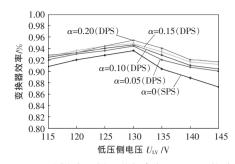


图 7 阶梯波调制下移相角与 MDCC 整体效率

Fig.7 Overall efficiency of MDCC with phase-shift angle under staircase triangular modulation

压比与 HFL 变压器变比吻合, 变换器整体效率最高;而随着低压侧电压偏离 130 V,MDCC 整体效率降低。此外,当  $\alpha \neq 0$ (DPS 控制)时,MDCC 的整体效率都比  $\alpha=0$ (SPS 控制)时高,并与  $\alpha$  成正比。因此,采用包含内移相角的阶梯波调制方式,可有效降低高频链电压 dv/dt、谐波和无功含量,提升 MDCC 的整体效率。

# 3 结语

本文分析了 MDCC 的 HFL 阶梯波调制方式。 采用傅里叶级数建模,可有效简化阶梯波调制的建 模和分析过程。相较于常用的方波调制方式,阶梯 波调制可有效减小 HFL 电压的 dv/dt,降低其谐波 和无功含量,提升 MDCC 的整体效率,更好地在直 流配电网中实现电压变换和电能传输。

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